

"The evolution of germ-soma specialization under different genetic and environmental effects"

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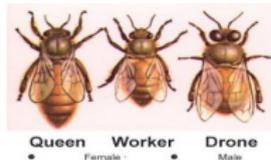
# Division of labor

- ▶ Germ-soma specialization in Volvocales, cyanobacteria, and hydrozoans;



- ▶ Specialization in carbon fixation and nitrogen fixation in cyanobacteria;

- ▶ Casts in social insects;



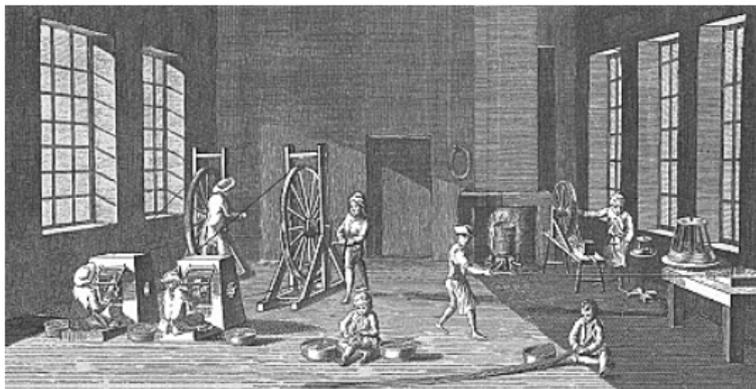
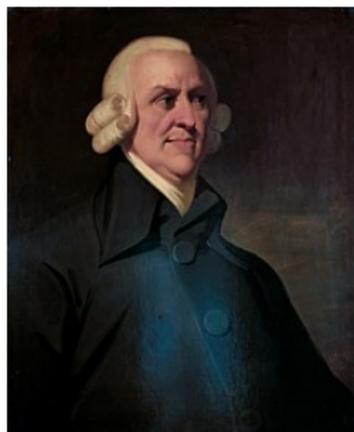
- ▶ Sexual division of labor in small hunter-gatherer groups;



- ▶ Division of labor in complex societies.



## Division of labor in economic theory



# Germ-soma specialization

Germ-soma specialization    Reproductive altruism → Biological complexity

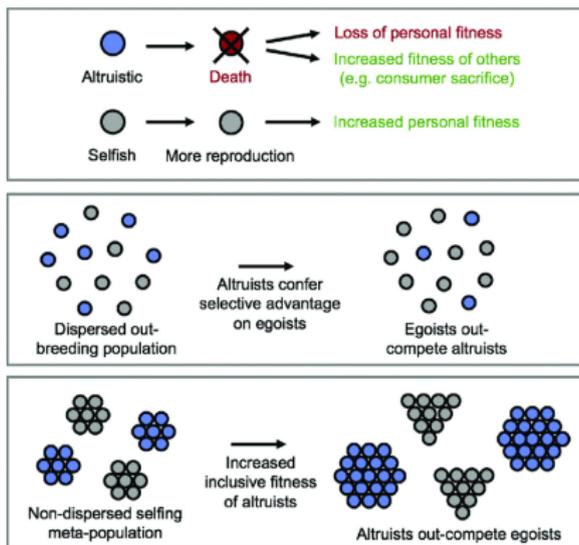
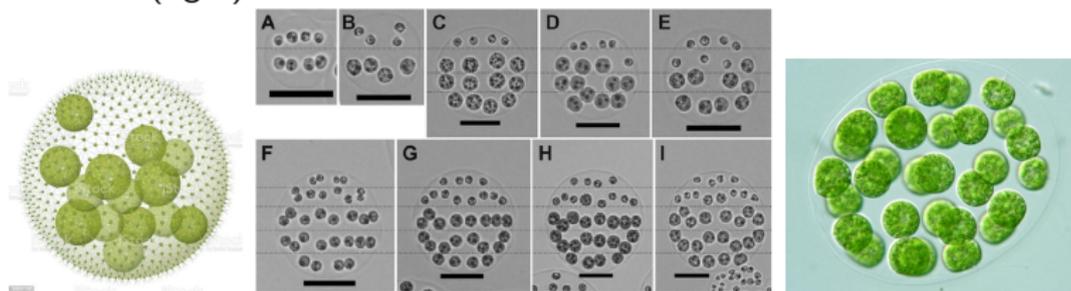


Figure: Lohr, J.N., Galimov, E.R. and Gems, D., 2019. Does senescence promote fitness in *Caenorhabditis elegans* by causing death?. *Ageing Research Reviews*, 50, pp.58-71.



## Effects of microenvironmental conditions on germ-soma specialization. Examples:

- ▶ Oxygen and nutrient gradients in biofilms;
- ▶ Iron gradients in *S.coelicolor* colonies;
- ▶ Examples in volvocaleans green algae: *Volvox* (left), *Pleodorina* (middle), *Eudorina* (right)<sup>1</sup>:



<sup>1</sup>Pictures from:

- ▶ <https://www.istockphoto.com/vector/volvox-gm959301582-261956197>
- ▶ Herron, M.D., Ghimire, S., Vinikoor, C.R. and Michod, R.E., 2014. Fitness trade-offs and developmental constraints in the evolution of soma: an experimental study in a volvocine alga. *Evolutionary ecology research*, 16(3), p.203.
- ▶ <https://alchetron.com/Eudorina>

## Mathematical models of the emergence of germ-soma specialization:

- ▶ Trade-offs between reproductive and somatic functions (Michod, 2006, Leslie et al., 2017),
- ▶ group size (Michod, 2006),
- ▶ genetic relatedness (Cooper and West, 2018),
- ▶ developmental plasticity (Gavrilets, 2010),
- ▶ positional effects (Reufferer and Wagner, 2012), ,
- ▶ topological constraints (Yanni et al., 2020),
- ▶ resource constraint, positional effects, and the trade-off curvature (Tverskoi et al., 2018)

## The model

We examine effects of environmental factors, positional effects and the trade-off between cell activity and fecundity on the evolution of germ-soma specialization in cell colonies.

Environmental effects in the model:

- ▶ At a between-colony level (resource-based competition)
- ▶ At a within-colony level (different microenvironmental effects on gene expressions)

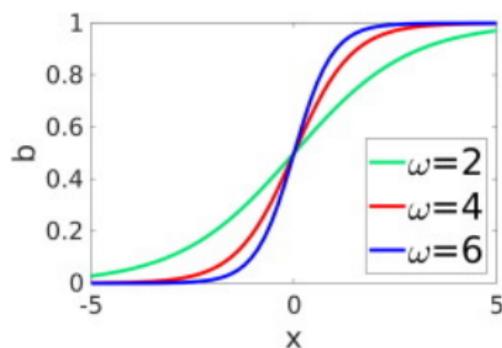
## The model: a general outline

- ▶ A finite population of colonies each composed by  $S$  asexually reproducing haploid cells,
- ▶ gene effects are affected by variation in microenvironment experienced by individual cells within a colony,
- ▶ colonies compete for resources,
- ▶ colonies surviving to the stage of reproduction disintegrate and the released cells start new daughter-colonies,
- ▶ mutation occurs during cell division.

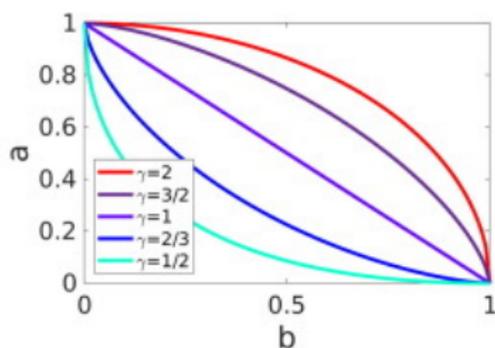
## The model: cell genotype and phenotype

- ▶ All cells within a colony are genetically identical. The cell's genotype is  $g = (g_1, \dots, g_G), g \in [0, 1]^G$ .
- ▶ These genes control a cell's activity  $a$  and fecundity  $b$ ,  $a, b \in [0, 1]$ .
- ▶ We define the  $i$ -th gene's effect on fecundity as  $x_i = e_i g_i$ , where  $e_i$  specifies microenvironmental effects. Microenvironment effects  $e_i$  may differ between different cells of the same colony.

## The model: cell genotype and phenotype



(a)

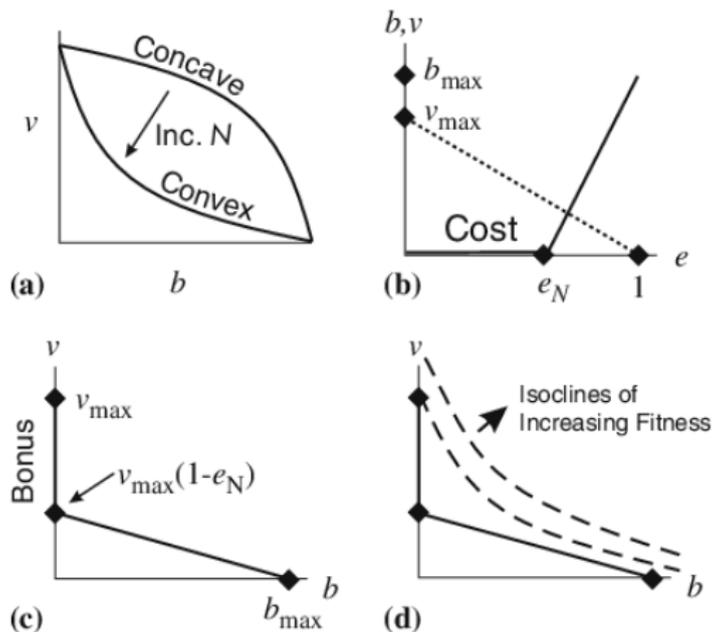


(b)

- ▶ We define a cell's fecundity as  $b = \frac{1}{1 + \exp\left(-\omega \frac{x}{\sqrt{G}}\right)}$ , where  $x = \sum x_i$  is the cumulative gene effect.
- ▶ Fecundity and activity within each cell are traded off:  $a = (1 - b^\gamma)^{\frac{1}{\gamma}}$ ,  $\gamma > 0$  controls the shape of the trade-off relation.

## Trade-off curvature and colony size

The trade-off function between activity and fecundity is convex-like for large-size colonies, and concave for small-size colonies.

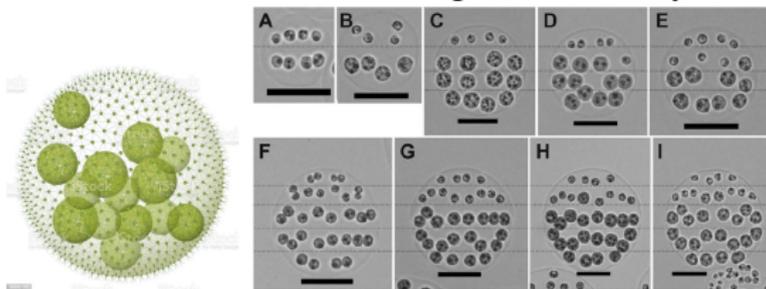


**Figure:** Michod, R.E., Viossat, Y., Solari, C.A., Hurand, M. and Nedelcu, A.M., 2006. Life-history evolution and the origin of multicellularity. *Journal of theoretical Biology*, 239(2), pp.257-272.

## Cell microenvironment and cell prototypes

Cells can differ in size or position in the colony, which can impact on their gene effect on fecundity.

- ▶ In *Volvox* the *regA* gene  $\downarrow$  reproduction in small cells (proto-soma), the *lag* gene  $\downarrow$  motility in large cells (proto-germ).
- ▶ In *Pleodorina starrii*, cells are divided into tiers arranged from the anterior to the posterior of determined according to the motility direction.<sup>2</sup>



A colony consists of groups of cells experiencing the same  $e = (e_1, \dots, e_G)$ , and cells belonging to different groups are characterized by different vectors  $e$ . Cells in the same group have the same *prototype*, and cells of different groups have different prototypes ( $s$  is the number of prototypes).

<sup>2</sup>Pictures from:

- ▶ <https://www.istockphoto.com/vector/volvox-gm959301582-261956197>
- ▶ Herron, M.D., Ghimire, S., Vinikoor, C.R. and Michod, R.E., 2014. Fitness trade-offs and developmental constraints in the evolution of soma: an experimental study in a volvocine alga. *Evolutionary ecology research*, 16(3), p.203.

## Cell microenvironment and cell prototypes

Two ways of specifying microenvironmental effects  $e_{mi}$   
( $m = 1, \dots, s; i = 1, \dots, G$ ):

- ▶ **Random microenvironmental effects.**  $e_{m,i}$  is drawn randomly and independently from a uniform distribution on  $[-1, 1]$ .
- ▶ **Microenvironmental gradients,**  $e_{m,i}$  change according to some gradient along the anterior-posterior axis.  
 $|e_{m,i}|$  decreases geometrically at rate  $r$  with the distance  $m$  from the anterior layer:  $e_{m+1,i} = r e_{m,i}$  with  $|e_{1,i}| = d, d > 0$ .

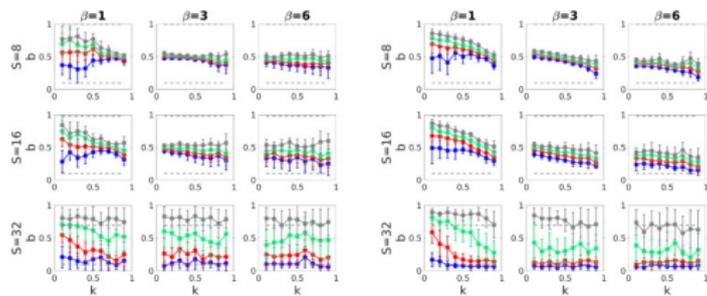
## Colony survival

- ▶ Colonies compete for a resource  $C > 0$ . The amount of the resource a colony secures in competition is  $R = C \cdot \frac{A^\beta}{\sum A^\beta}$ , where  $A = \sum_j a_j$ ,  $\beta \geq 1$  is the strength of competition.
- ▶ The colony always survives to the stage of reproduction if  $R \geq R_0$ . If  $R < R_0$ , the probability of survival is  $V = R/R_0$ , where  $R_0 = (1 - k)A + kB$  and  $0 < k < 1$  measures the relative cost of fertility.

## Other details

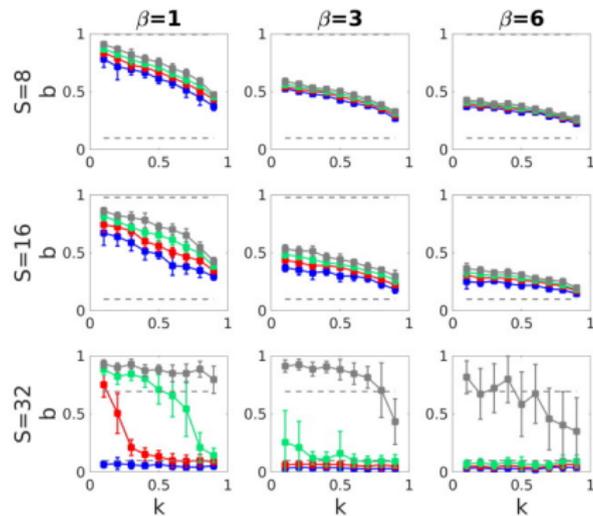
- ▶ **Reproduction.** Each surviving colony disintegrates into  $S$  cells and each cell seeds a new colony with probability  $b_j$ . Mutations in an offspring colony genotype  $g$  happen with probability  $\mu$  per gene.
- ▶ We define *a cell phenotype* as its fecundity  $b$ . Cells of the same prototype have the same phenotype. Cells of different prototypes can have the same phenotype as well.  $\rightarrow$  the number of different cell phenotypes  $M \leq s$ .

# Results: random microenvironmental effects



(a)  $G = 2$

(b)  $G = 8$



(c)  $G = 32$

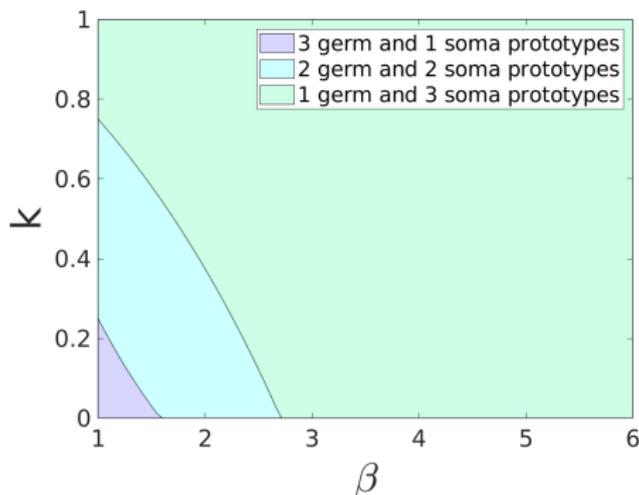
## Some analytical results

Analytical approximations (for  $G \rightarrow \infty$ ) show that

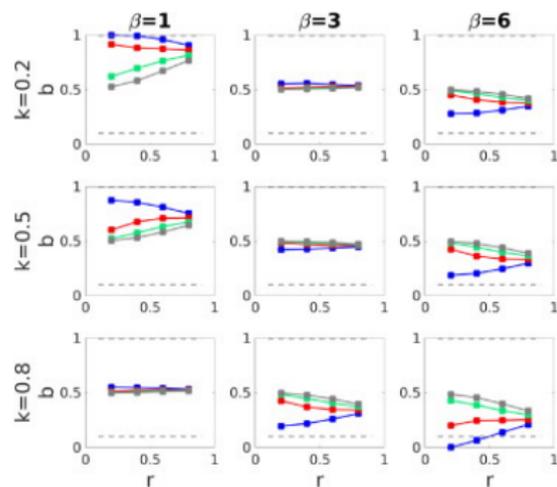
- ▶ In the case of concave trade-offs and random microenvironmental effects, equilibrium cell fecundity  $b^*$  can be found as

$$\frac{k\beta}{1-k} \cdot b^{*\gamma+1} = (1 - \beta b^{*\gamma}) \cdot (1 - b^{*\gamma})^{\frac{1}{\gamma}}.$$

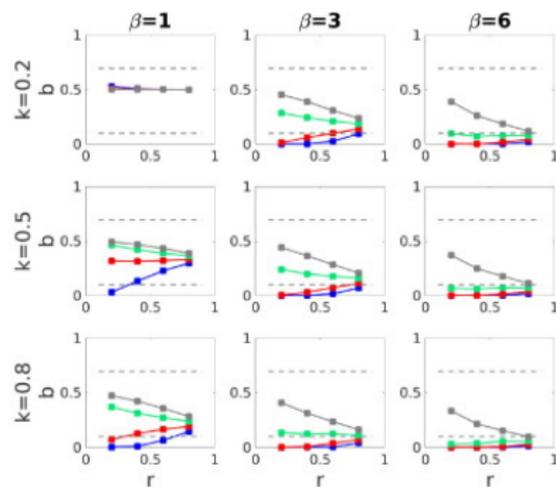
- ▶ In the case of convex trade-offs, all prototypes or all prototypes except one are specialized.



## Results: single gradient



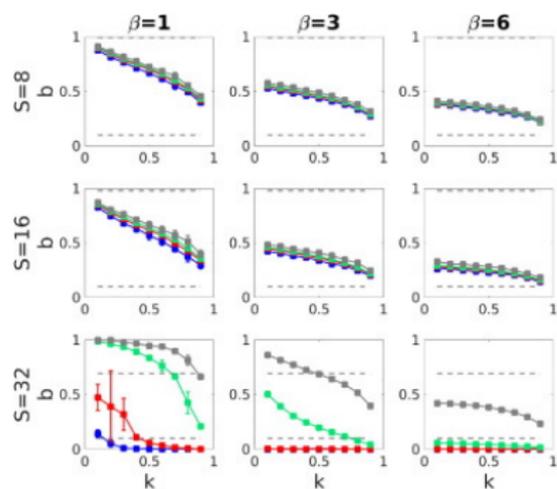
(a)  $S = 8$



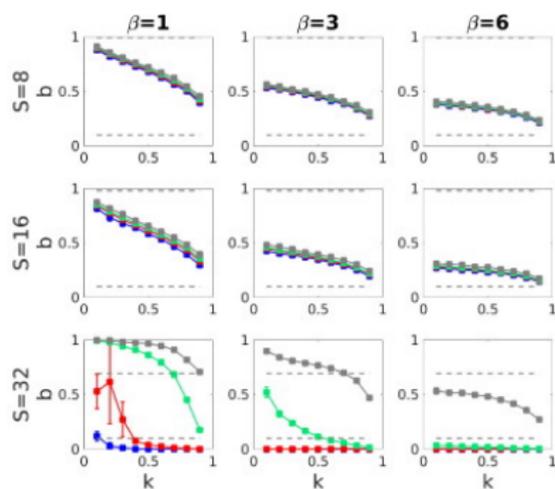
(b)  $S = 32$

Cell prototypes are marked in blue, red, green and gray colors respectively along the anterior-posterior axis.

## Results: several gradients



(a)  $G = 8$



(b)  $G = 32$

Prototypes are sorted by increasing fecundity and marked with different colors.

## Summary of the results

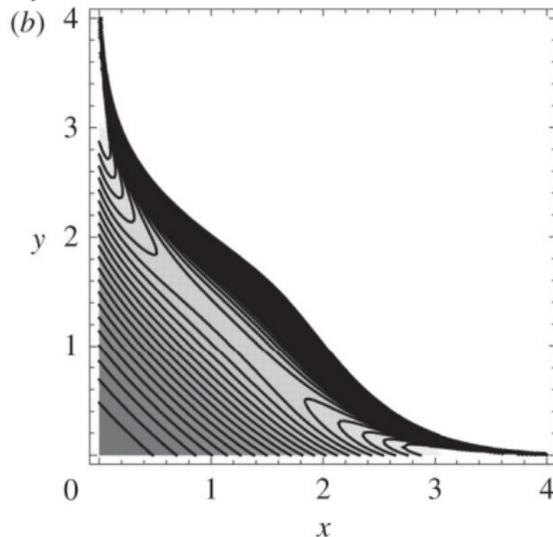
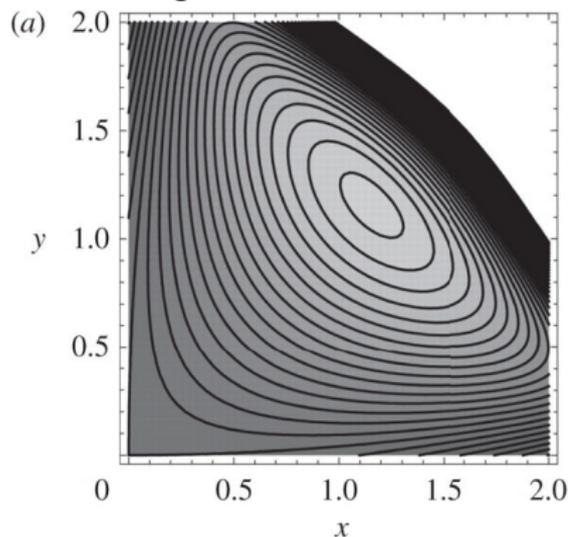
ME	Size	G	Typical patterns of within-colony differentiation	Conditions for coexistence of reproductive and somatic cells
R	S	L	One type of unspecialized cells	-
		S	One or two types of unspecialized cells	-
	L	L	Two types of cells: somatic and reproductive or somatic and unspecialized	All cases except one with large $k$ and $\beta$
		S	Three types of cells: somatic, reproductive and unspecialized	Can be observed for all $k$ and $\beta$ , conditions are determined by random microenvironmental effects
1G	S	S&L	One type of unspecialized cells, or 2 types of cells (somatic and unspecialized or reproductive and unspecialized)	-
	L	- " -	One type of unspecialized cells, or 2 types of cells (somatic and unspecialized or 2 unspecialized) or 3 types of cells (somatic and 2 unspecialized)	-
SG	S	- " -	One type of unspecialized cells	-
	L	- " -	Two types of cells (somatic and reproductive or somatic and unspecialized) or three types of cells (somatic, reproductive and unspecialized)	$\beta$ is not large and $k$ is not large

## Some conclusions

- ▶ Specialization can evolve even if the curvature of the trade-off is concave. Incomplete specialization or even colonies composed only by unspecialized cells can be observed in the case of a convex trade-off.
- ▶ The type and extent of variation in within-colony microenvironment and, in the case of random microenvironment, the number of genes involved, are key factors shaping the model dynamics

## Some conclusions

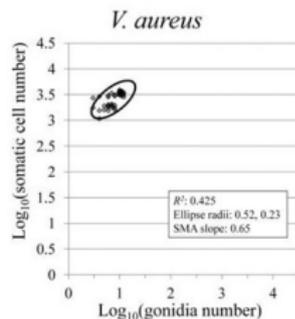
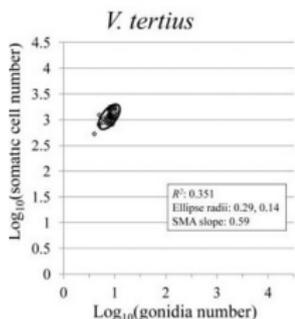
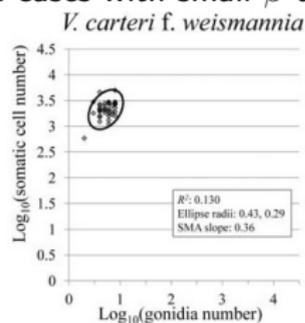
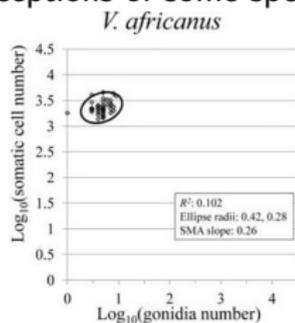
Increasing  $s \rightarrow \uparrow W$ . This happens because  $\uparrow s \rightarrow \uparrow$  in the dimensionality of phenotype space. This generates a fitness landscape with a new fitness maximum, in which colony phenotypes that are fitness optimal for smaller number of gradients become fitness saddle points.



Pictures from: Ispolatov, I., Ackermann, M. and Doebeli, M., 2012. Division of labour and the evolution of multicellularity. *Proceedings of the Royal Society B: Biological Sciences*, 279(1734), pp.1768-1776.

## Some conclusions

The share of reproductive cells in large colonies is smaller than that of somatic cells, with the exceptions of some special cases with small  $\beta$  and  $k$ .



Pictures from: Shelton, D.E., Desnitskiy, A.G. and Michod, R.E., 2012. Distributions of reproductive and somatic cell numbers in diverse Volvox (Chlorophyta) species. Evolutionary ecology research, 14, p.707.

Thank you for your attention!